

# Knowledge Transfer through Value Function for Compositional Tasks

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# Motivation

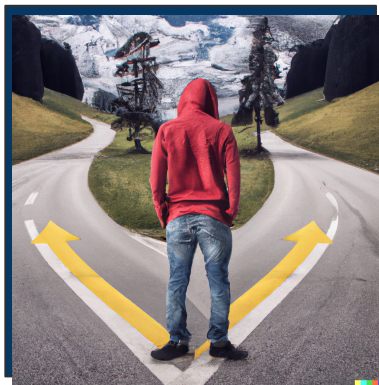
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# Exploration is hard!

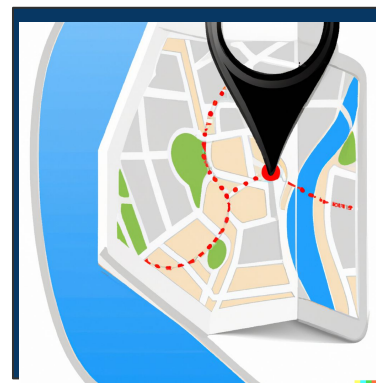
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Sparse and binary  
outcomes



Multiple objectives



High-dimensional  
state spaces

# Curriculum Learning [Bengio et al. 2009]

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$$1 + 1 + 1 = 3$$

$$5 - 1 - 2 = 2$$

$$7 - 3 + 4 = 8$$

$$3 \times 1 = 3$$

$$5 \times 1 - 3 = 2$$

$$8 \div 2 \times 2 = 8$$

$$3 \times (1 + 3) = 12$$

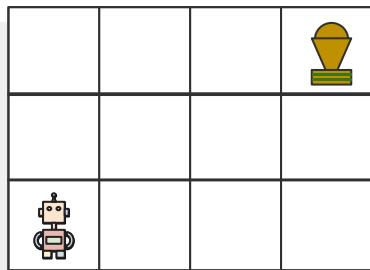
$$7 \div 2 = 3.5$$

$$x \div 2 = 8 + 4$$

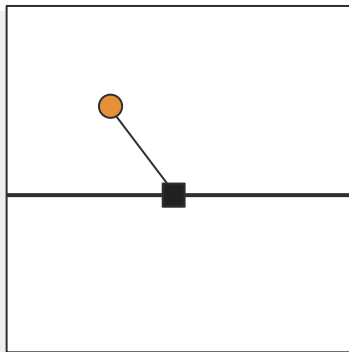
Task Complexity



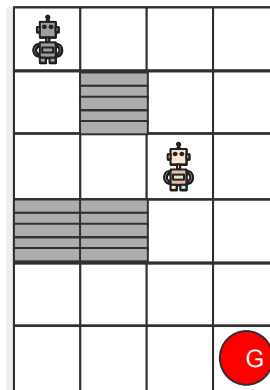
# Making tasks easier: MDP degrees of freedom



Reward shaping \*



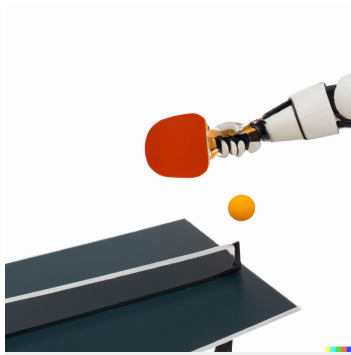
Transition probability



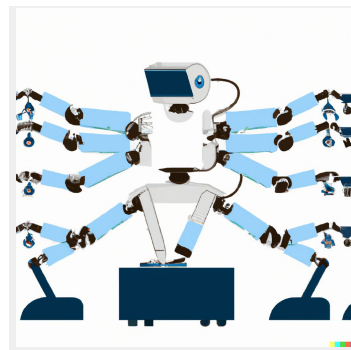
Initial state distribution

# Making tasks easier: MDP degrees of freedom

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States



Actions

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# Knowledge Transfer for Compositional Representations

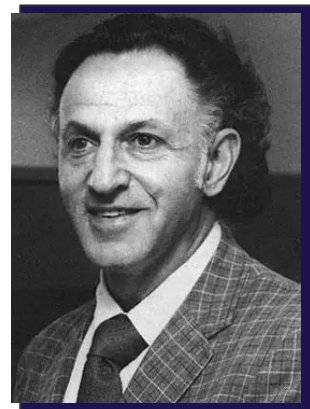
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# Q-Learning [Watkins & Dayan (1992)]

$Q(s,a)$  How good is being in a state  $s$  and performing an action  $a$ ?

$$Q(s, a) = Q(s, a) + \alpha \underbrace{[R(s, a) + \gamma \max_{a'} Q(s', a') - Q(s, a)]}_{\text{TD error}}$$

Target value



*Richard Bellman*

*state*

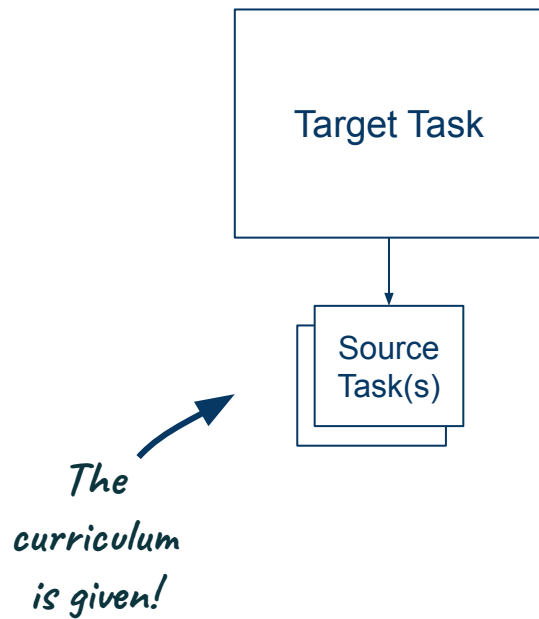
1.234	1.434	1.434	...
0.234	...		
...			

*action*



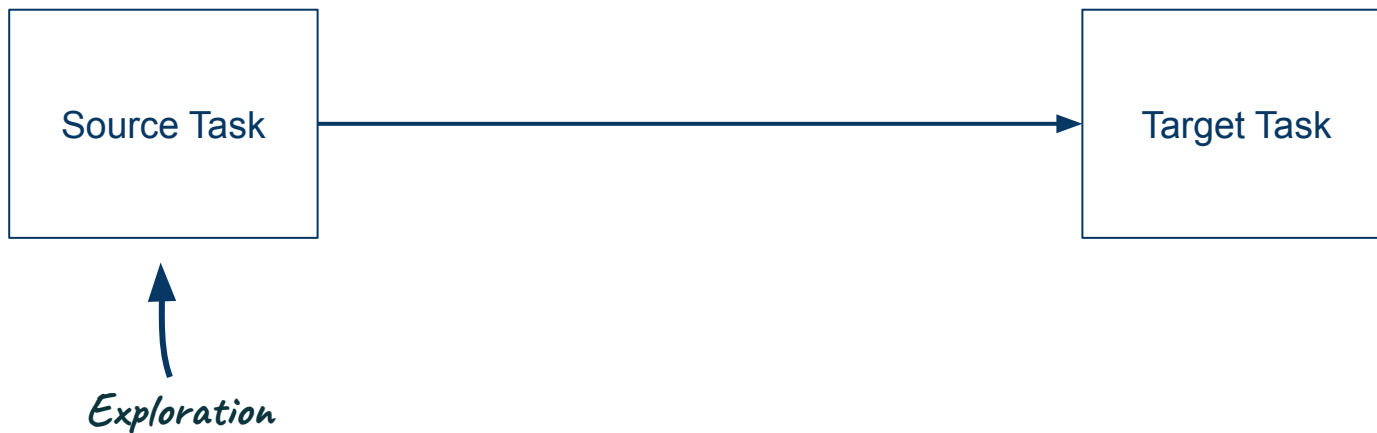
# Knowledge Transfer for Compositional Representations

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# Knowledge Transfer for Compositional Representations

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# Knowledge Transfer for Compositional Representations

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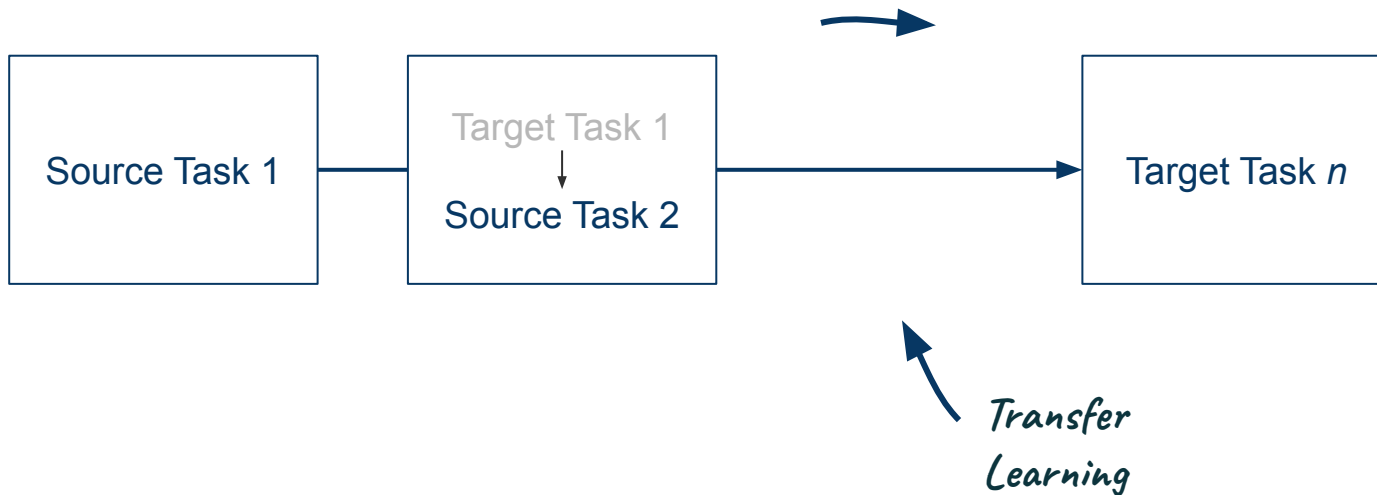


*Transfer Learning*

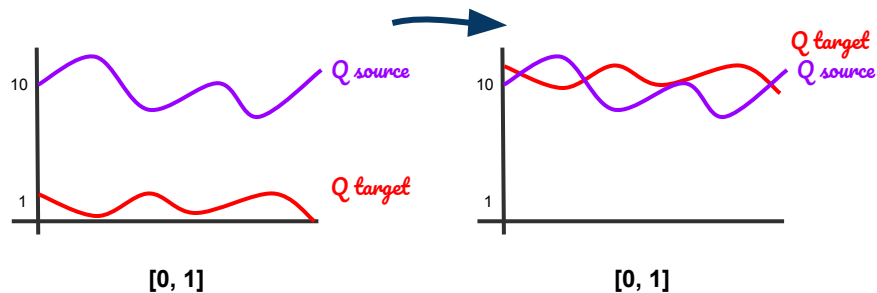
$$a = \begin{cases} \text{softmax}(\{\max(Q_s), \max(Q_t)\}) \\ \text{argmax}(Q_s), \text{softmax}_{Q_s} \\ \text{argmax}(Q_t), \text{softmax}_{Q_t} \end{cases}$$

# Knowledge Transfer for Compositional Representations

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# Knowledge Transfer for Compositional Representations



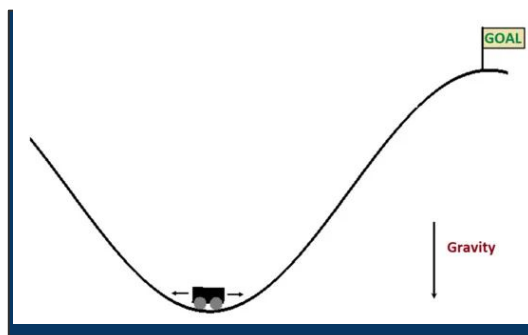
$$a = \begin{cases} \operatorname{softmax}(\{ \max(Q_s), \max(Q_t) \}) \\ \operatorname{argmax}(Q_s), \operatorname{softmax}_{Q_s} \\ \operatorname{argmax}(Q_t), \operatorname{softmax}_{Q_t} \end{cases}$$

*Allow target task policy play its own actions*

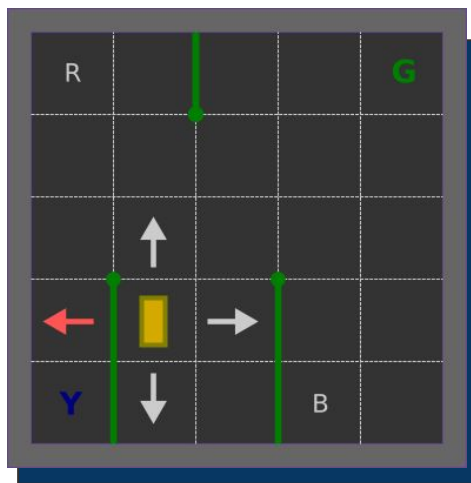
*Mitigate distributional shift*

# Proof-of-concept

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*Mountain Car*

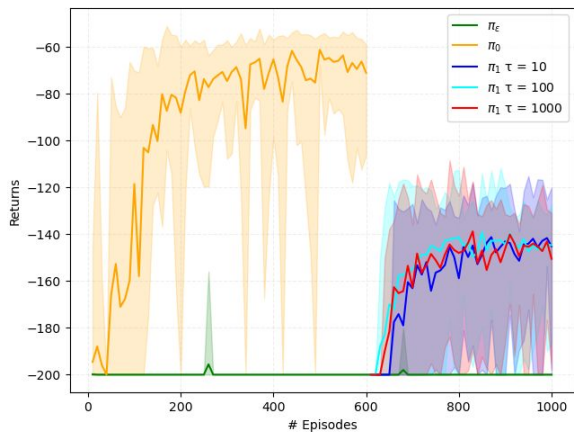


*Taxi cab*

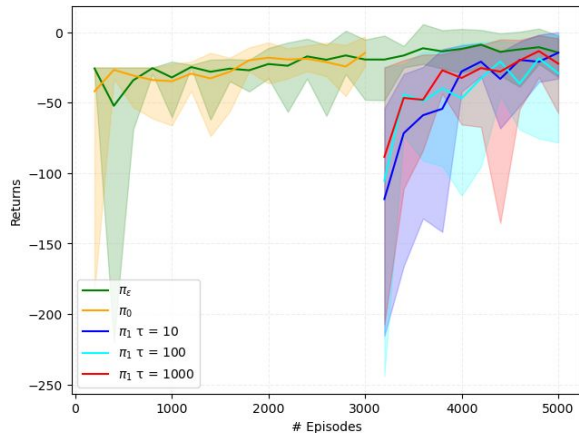


*Frozen Lake*

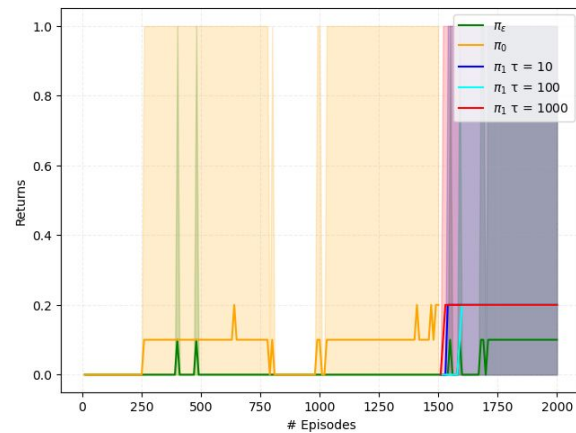
# Results



*Mountain Car*



*Taxi cab*



*Frozen Lake*

# Acknowledgments

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